A Richardson-Lucy Algorithm Using A Varying Point Spread **Function Along The Iterations**

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Image restorations with the Richardson-Lucy [1-2] algorithm suffer the drawback imposed by the constraint of a constant Point Spread Function – PSF as unfolding function. Indeed, as the iterations proceed, the overall resolution is improved while the PSF is kept constant. This mismatch is eliminated in this work by reducing the PSF width as the iterations proceed. Such a procedure requires the resolution of the image so far achieved, which is performed with an algorithm based upon the concept of Global Contrast (G-value for short) [3]. This algorithm is not tied to any type of acquisition system, as it uses solely the information provided by the image itself. The G-value increases with w, reaches a maximum, and then decreases again. The w-value yielding the maximum G is assigned as the best PSF width. The G-value is determined as follows:

$$G = \left[\sum_{i=1}^{M} \sum_{j=1}^{N} u(i,j) \cdot \beta(i,j) \right] \cdot \left[\sum_{i=1}^{M} \sum_{j=1}^{N} u(i,j) \cdot \left| 1 - \beta(i,j) \right| \right]^{-1}$$
 (1)

$$\beta(i,j) = 0$$
 for $u(i,j) \le u_m$ (2)

$$\beta(i, j) = 1$$
 for $u(i, j) > u_m$ (3)

$$\beta(i,j) = 1 \quad \text{for } u(i,j) > u_{\text{m}}$$
(3)
$$u_{m} = (M.N)^{-1} \cdot \sum_{i=1}^{M} \sum_{j=1}^{N} u(i,j)$$
(4)

u(i,j) = Pixel value at the point (i,j).

M, N = No. of columns and lines of the image

After equation (4), u_m is the average pixel-value used to classify all pixels into two classes: below and above it. The sums of all pixelvalues occurring above and below u_m constitute the numerator and denominator of equation (1) respectively, defining the G-value, while the bump function $\beta(i, i)$ classifies the pixel-values as below or above u_m . A higher fraction of pixels at darker and brighter zones means a higher contrast arising from a better resolution. Therefore, the sum of all pixel-values above u_m

would increase while that below it would decrease, resulting into a higher G-value. Further details can be found elsewhere [4].

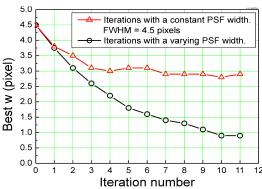


Figure 1. Behavior of *constant* x varying PSF.

As shown in Figure 1, the PSF drops faster for the varying approach demonstrating its higher effectiveness. The deconvolved gamma-ray radiographs in Figure 2 corroborate this outcome.

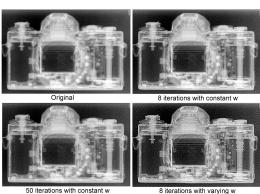


Figure 2. Original and unfolded images. Eight iterations with a varying PSF outperform those with a constant value, even for 50 iterations.

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